



Universitat de Lleida

# DEGREE CURRICULUM

# **COMPUTATIONAL MODELS AND COMPLEXITY**

Coordination: VALLS MARSAL, MA MAGDALENA

Academic year 2021-22

## Subject's general information

Subject name	COMPUTATIONAL MODELS AND COMPLEXITY			
Code	102065			
Semester	2nd Q(SEMESTER) CONTINUED EVALUATION			
Typology	Degree	Course	Character	Modality
	Bachelor's Degree in Computer Engineering	3	COMPULSORY	Attendance-based
	Bachelor's Degree in Computer Engineering	3	OPTIONAL	Attendance-based
Course number of credits (ECTS)	4.5			
Type of activity, credits, and groups	Activity type	PRAULA		TEORIA
	Number of credits	3		1.5
	Number of groups	1		1
Coordination	VALLS MARSAL, MA MAGDALENA			
Department	MATHEMATICS			
Teaching load distribution between lectures and independent student work	4,5 ECTS correspond to a workload of 45 h of lectures and assesment and 67 h of autonomous study work for each student.			
Important information on data processing	Consult <a href="#">this link</a> for more information.			
Language	Catalan			
Distribution of credits	There is a single group with 4.5 ECTS, where theoretical lectures are combined with more applied ones.			

Teaching staff	E-mail addresses	Credits taught by teacher	Office and hour of attention
MIRET BIOSCA, JOSE MARIA	josepmaria.miret@udl.cat	1,5	
VALLS MARSAL, MA MAGDALENA	magda.vallsmarsal@udl.cat	3	

## Subject's extra information

Previous knowledge on the subjects *Algebra*, *Computational Logics and Algorithmics and Complexity*, *Discrete Mathematics and Languages*, *Automata and Grammars* is recommended.

This subject is scheduled in the spring semester of the 3rd year, in the especialization on *Computation*.

The knowledge and competencies adquired in this subjects will be useful to follow other subjects in the same especialization, and in particular for the subject *Language Processing Algorithms*.

## Learning objectives

- Understand the basic Turing machine model, its relationship with the finite automata and possible extensions of this model.
- Design Turing machines as language recognizers or as function calculators.
- Distinguish between recursively enumerable and recursive languages, and know their properties.
- Get some examples of non-recursive languages.
- Understand the concept of reduction between languages and be able to give reduction functions.
- Understand the relationship between recursive / recursively enumerable languages and decidable / undecidable problems.
- Distinguish between complexity of an algorithm and complexity of a problem.
- Recognize the different kinds of complexity of a problem: P, NP-complete, NP

## Competences

### Specific competences

- GII-C1 - Capacity to have a deep knowledge of the basic principles and models for computation and to know how to apply them in order to interpret, select, value, model, and create new concepts, theories, uses and technological developments related with the informatics.
- GII-C3 - Capacity to evaluate the computational complexity of a problem, to know the algorithmic strategies that can drive to its solving and recommend, develop and implement the one which guarantee the best performance in accordance with the requirements.

### Cross-disciplinary competences

- EPS6 - Capacity of analysis and synthesis.

### University strategic competences

- CT2 - Mastering a foreign language, especially English.
- CT3 - Training experience in the use of the new technologies and the information and communication technologies.

## Subject contents

### 1. Turing machines

- Basic Turing machine model.
- Extensions on the basic Turing machine model.
- Turing machine as languages recognizer.
- Turing machine as function calculator.
- Algorithms and Turing machines.
- Church-Turing thesis.
- Gödel number of a Turing machine.
- Universal Turing machine.

### 2. Recursive languages

- Recursive and recursively enumerable languages.
- Operations with recursive languages.
- Operations with recursively enumerable languages.
- The halting problem.

### 3. Reductions

- Reductions between languages.
- Properties of the reductions.

### 4. Undecidability

- Decidable and undecidable problems.
- Undecidable problems on Turing Machines: the halting problem and the belonging problem
- PCP, the Post correspondence problem.

### 5. Complexity

- Classes of complexity.
- Reductions between problems in polynomial time.
- SAT, the satisfiability problem.
- Other NP-complete problems.
- $P = NP?$

## Methodology

Lectures combine theoretical concepts with practical ones. The lectures present the basics of the subject, incorporating illustrative examples that facilitate its understanding. In the classes of problems we combine joint resolution on the board, individual resolution and group resolution.

Students prepare an extension work related with some topics on Theoretical Computer Science. The students have to search for appropriate bibliography and they have to analyze it. The work is presented and discussed in the classroom, with all the students and teachers.

Depending on guidelines given by health authorities, lectures could be developed in a mixed model: if so, theoretical lectures would be given on-line, while problem solving lessons would be held in the classroom.

## Development plan

Week	Lesson	Activities	Student workload
1	Introduction. Lesson 1		2 hours. Study and problem solving.
2	Lesson 1		3 hours. Study and problem solving.
3	Lesson 1	Work topic assignment	3 hours. Study and problem solving.
4	Lesson 2		3 hours. Study and problem solving. Work development.
5	Lesson 2		3 hours. Study and problem solving. Work development.
6	Lesson 2		4 hours. Study and problem solving. Work development.
7	Lesson 3		4 hours. Study and problem solving. Work development.
8	Lesson 3		5 hours. Study for exams.
9		Partial 1 Assesment	6 hours. Study for exams.
10	Lesson 4		3 hours. Study and problem solving.
11	Lesson 4		3 hours. Study and problem solving.
12	Lesson 4		4 hours. Study and problem solving. Prepare work presentation.
13	Lesson 5		4 hours. Study and problem solving. Prepare work presentation..
14	Lesson 5	Work presentation	4 hours. Study and problem solving.
15	Lesson 5		5 hours. Study for exams.
16		Tutorization	5 hours. Study for exams.
17		Partial 2 Assesment	6 hours. Study for exams.
18		Tutorization	
19		Final assesment	

## Evaluation

Acr.	Assessment activities	Weight	Minimum mark	Resit
P1	Partial 1. Lessons 1, 2.	4.5 points	1 point	YES
P2	Partial 2. Lessons 3, 4, 5.	4.5 points	1 point	YES
AC	Complementary activities : development and presentation of a work on complementary aspects	1 point	NO	NO
PCL	Participation	1 point	NO	NO

**FinalMark** = P1 + P2 + AC+ PCL

A student with final mark below 5 or who has not reached the minimum marks required, can resit either P1, P2 or both. Up to 1 additional point can be assigned, according to participation in the classroom and delivered problems.

## Bibliography

### Basic bibliography:

Josep M. MIRET; Magda VALLS. Recull de problemes de Models de Computació i Complexitat. Universitat de Lleida, 2012.

Maria José SERNA; Carme ALVAREZ; Rafel CASES; Antoni LOZANO. Els límits de la computació. indecidibilitat i NP-completesa. Edicions UPC, 2001.

### Complementary bibliography:

John HOPCROFT; Jeffrey ULLMAN. Introduction to Automata Theory, Languages and Computation. Addison-Wesley, 1979.

Dean KELLEY. Teoría de Autómatas y Lenguajes Formales. Prentice-Hall, 1995.

Jairo ROCHA; Francesc ROSSELLÓ. Autòmats i Llenguatges: verificació, implementació i concurrència. Materials didàctics 107, Universitat de les Illes Balears, 2003.

Michael SIPSER. Introduction to the theory of computation. Cengage Learning, 2013.